

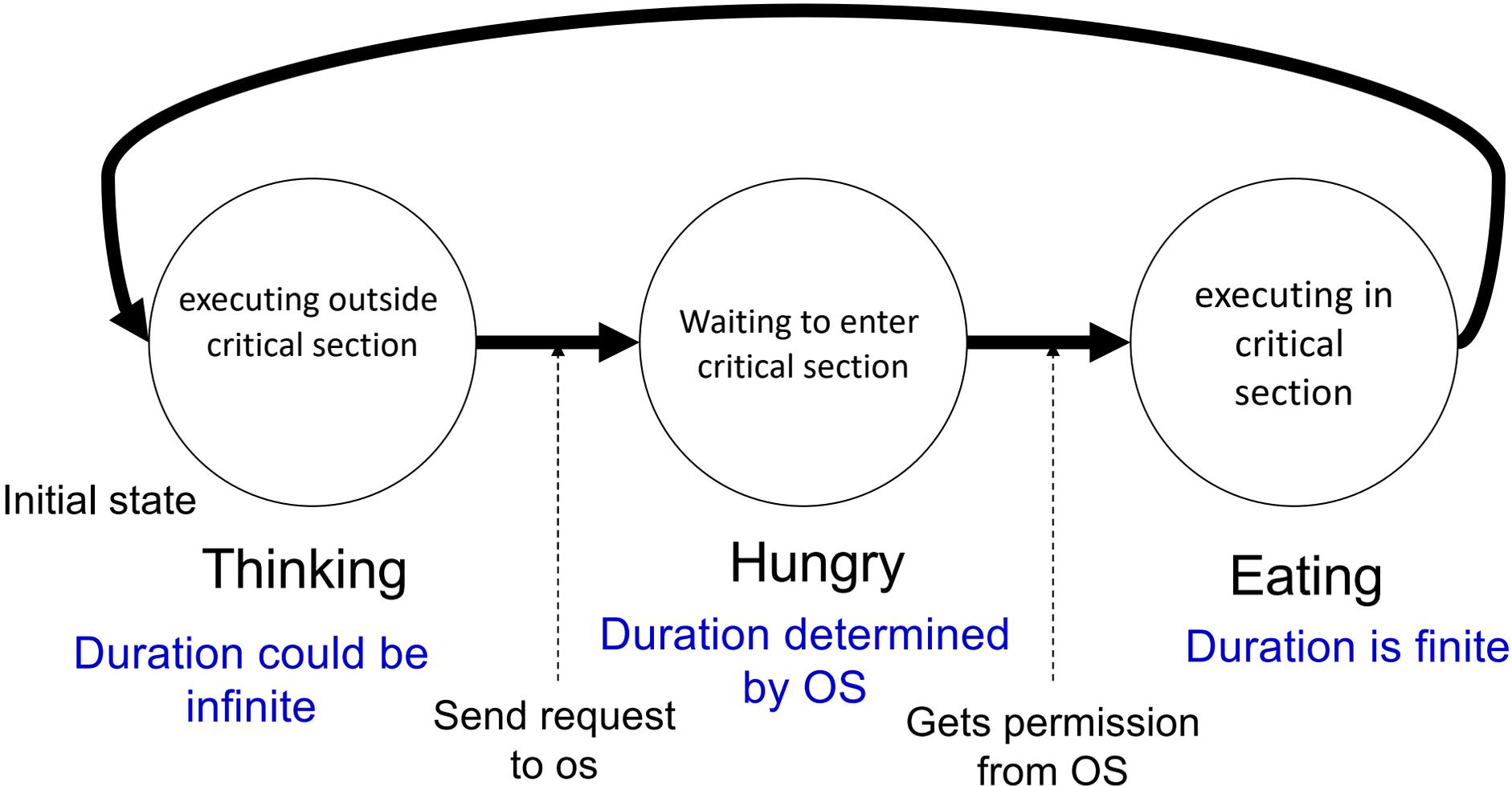
Caltech, CMS. CS/IDS 142: Lecture 6.1  
Distributed Dining Philosophers  
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4 November 2019

**Goals:**

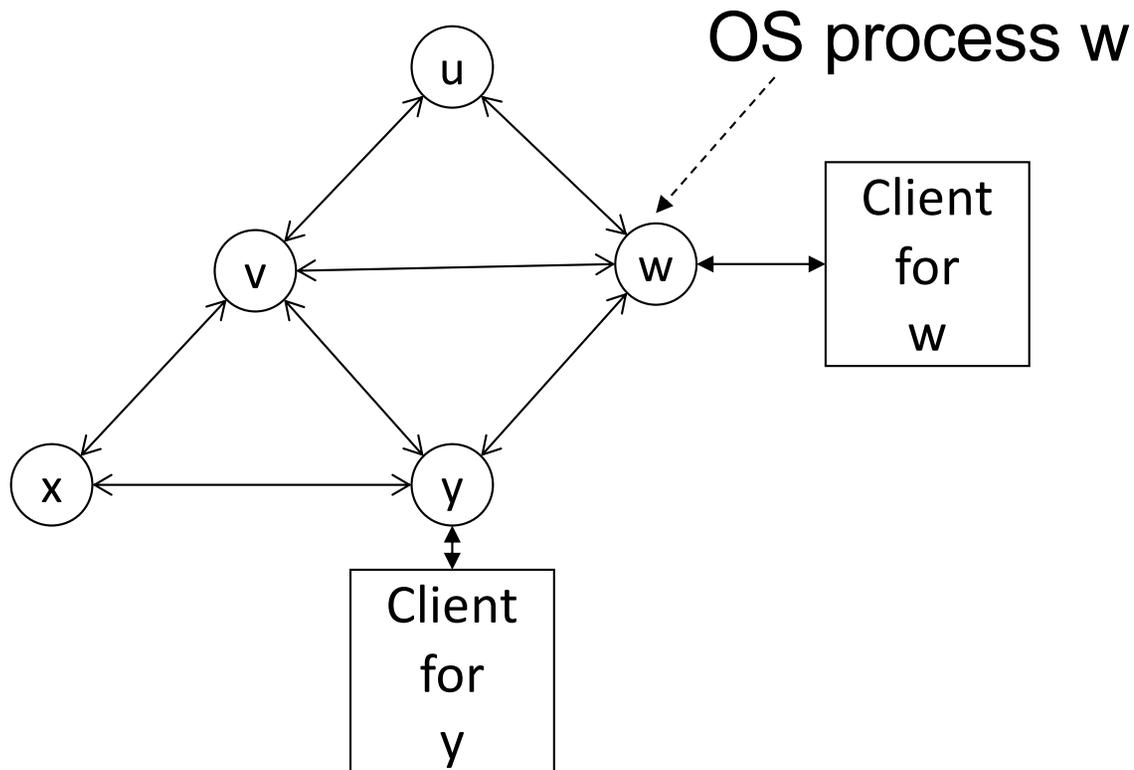
1. **Conflict resolution** in distributed systems: Previously: mutual exclusion. Today Distributed Dining Philosophers.
2. **Dynamically changing graphs** to design distributed algorithms. This lecture: Priority Graphs. Earlier lectures: Tree for Diffusing Computation. Snapshot: timeline graph.
3. Use of **tokens** and other invariant structures.

**Reading:** Sivilotti, Chapter 8

# Client Life Cycle: Same as for mutex



Given: Undirected graph. Each node consists of an OS process and a client process



**Specification:**

**Always:** Neighboring clients are not in critical sections.

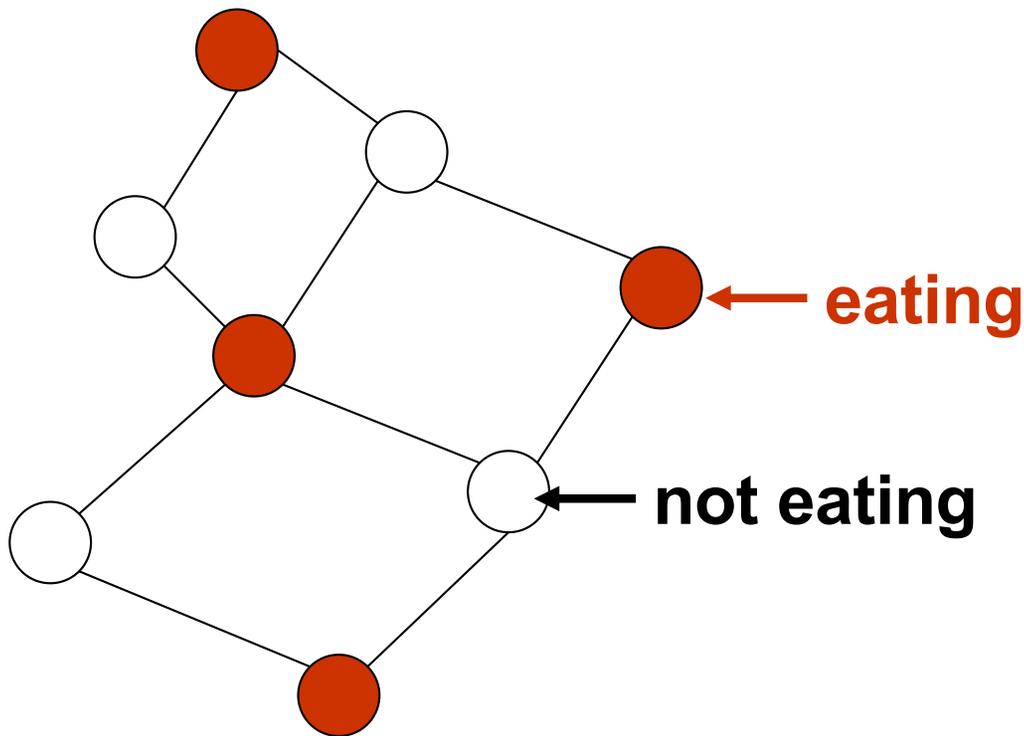
**Eventually:** Every client waiting to enter its critical section does so.

**Given:** Clients remain in critical sections for finite time.

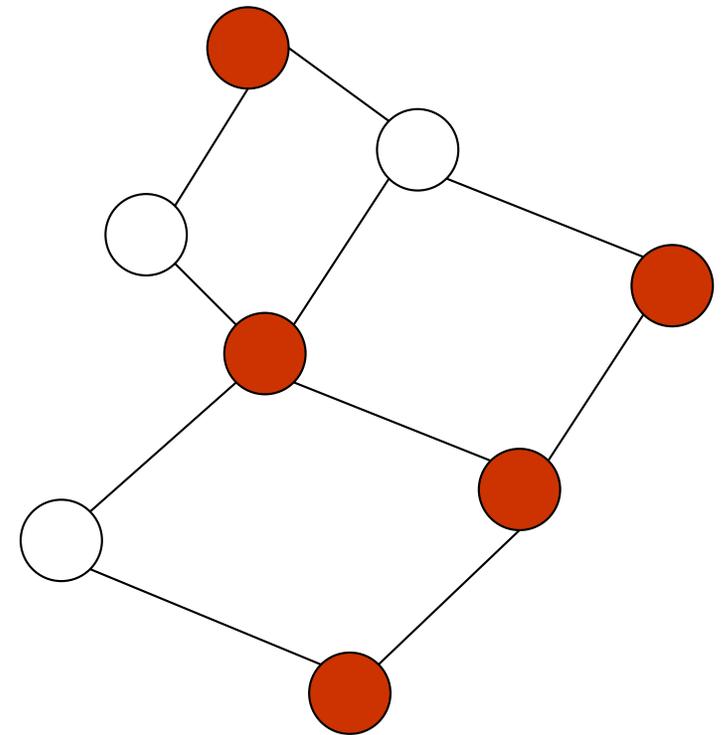
Channels between neighbors.

# Focus on OS: Client code is straightforward

## Safety property: Always neighbors aren't eating



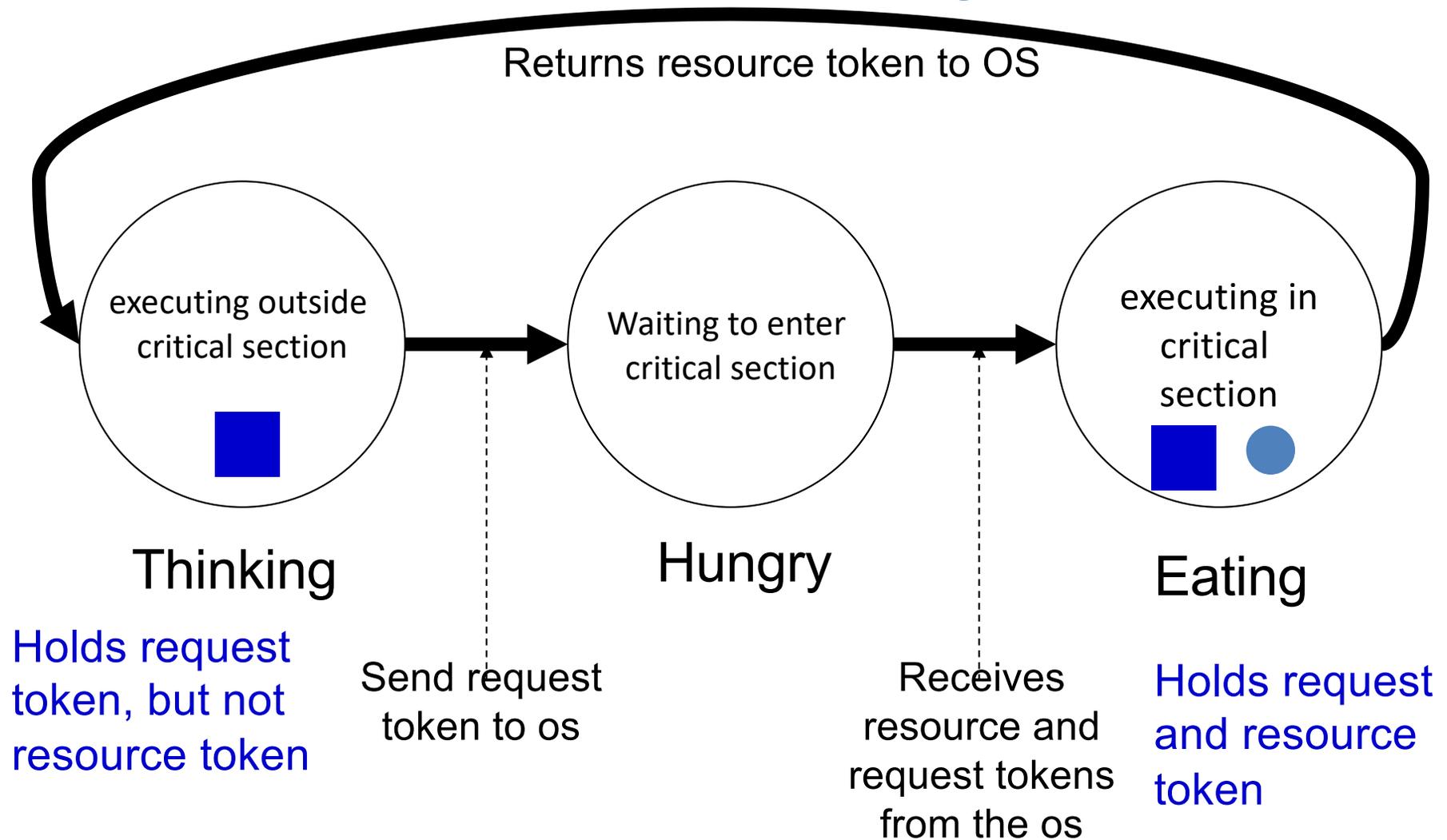
Safety property:  
Neighbors aren't eating



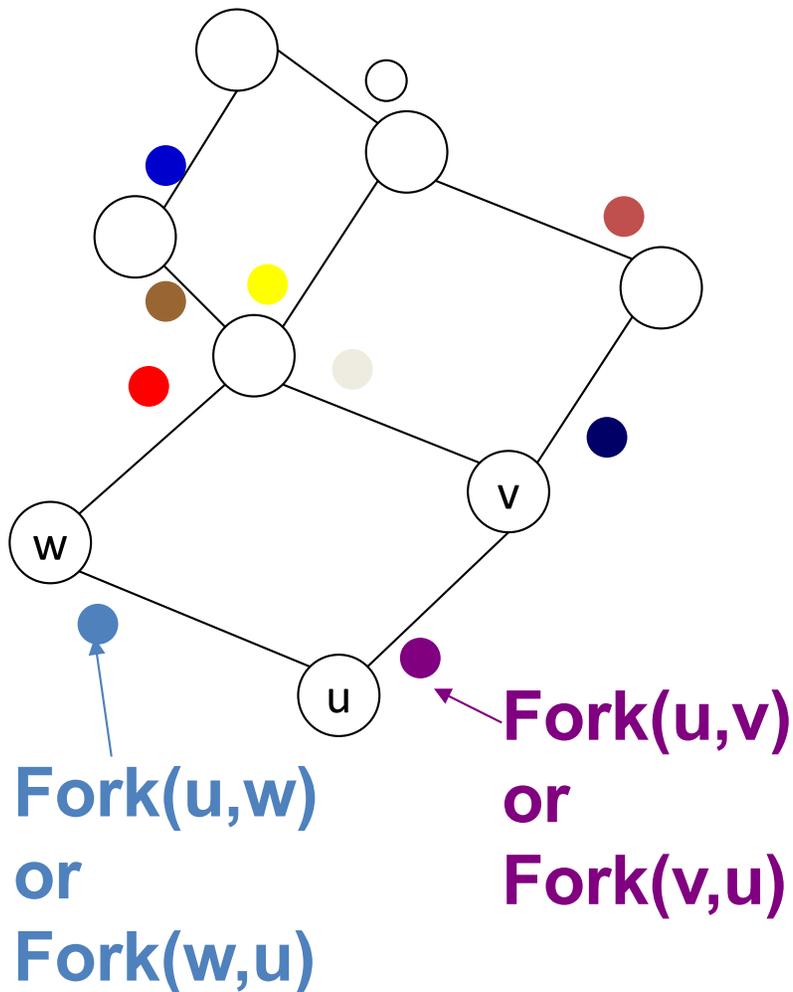
Safety property violated:  
Neighbors are eating

# Client to OS messages: Tokens: example of an invariant structure

request token: ■  
resource token: ●



# Another example of tokens: Introduction of forks

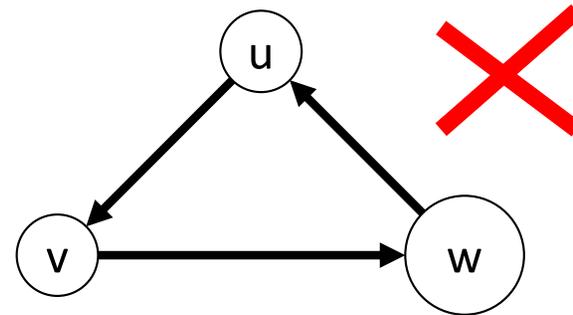
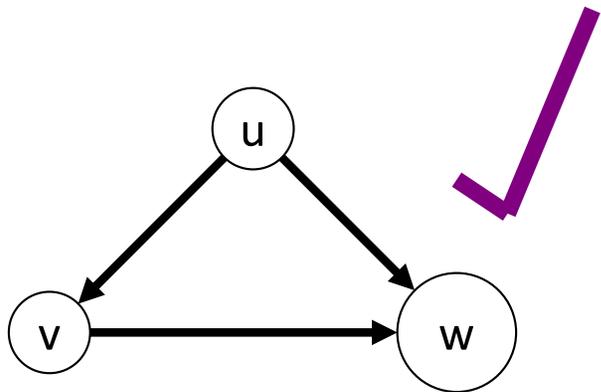


- There is exactly one fork on each edge.
- Forks on different edges have different colors: Color  $(u,v)$  is different from color  $(u,w)$ .
- A fork on an edge  $(u, v)$  is at  $u$  or at  $v$  or in the channel from  $u$  to  $v$  or in the channel from  $v$  to  $u$ .
- Philosopher eats only if it holds all its forks.
- Safety property satisfied

**Conflict resolution** What to do when  $u$  and  $v$  want  $\text{fork}(u,v)$  at the same time?

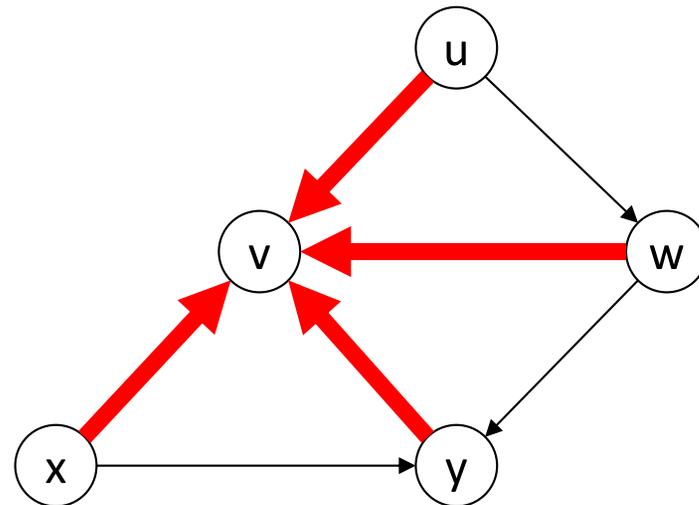
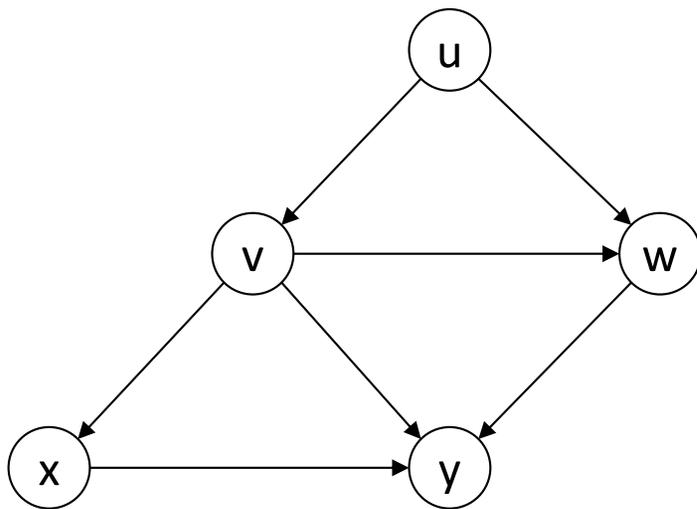
**Priority:** Give the fork to the agent with higher priority.

- The vertices of a priority graph represent agents.
- The directed edges represent priority. There is an edge  $(u, v)$  exactly when agent  $u$  has priority over agent  $v$ .
- Maintain the invariant that the priority graph is acyclic. Why? Because a symmetric state can persist forever.



# How should priorities change when a process eats?

v holds all its forks and eats



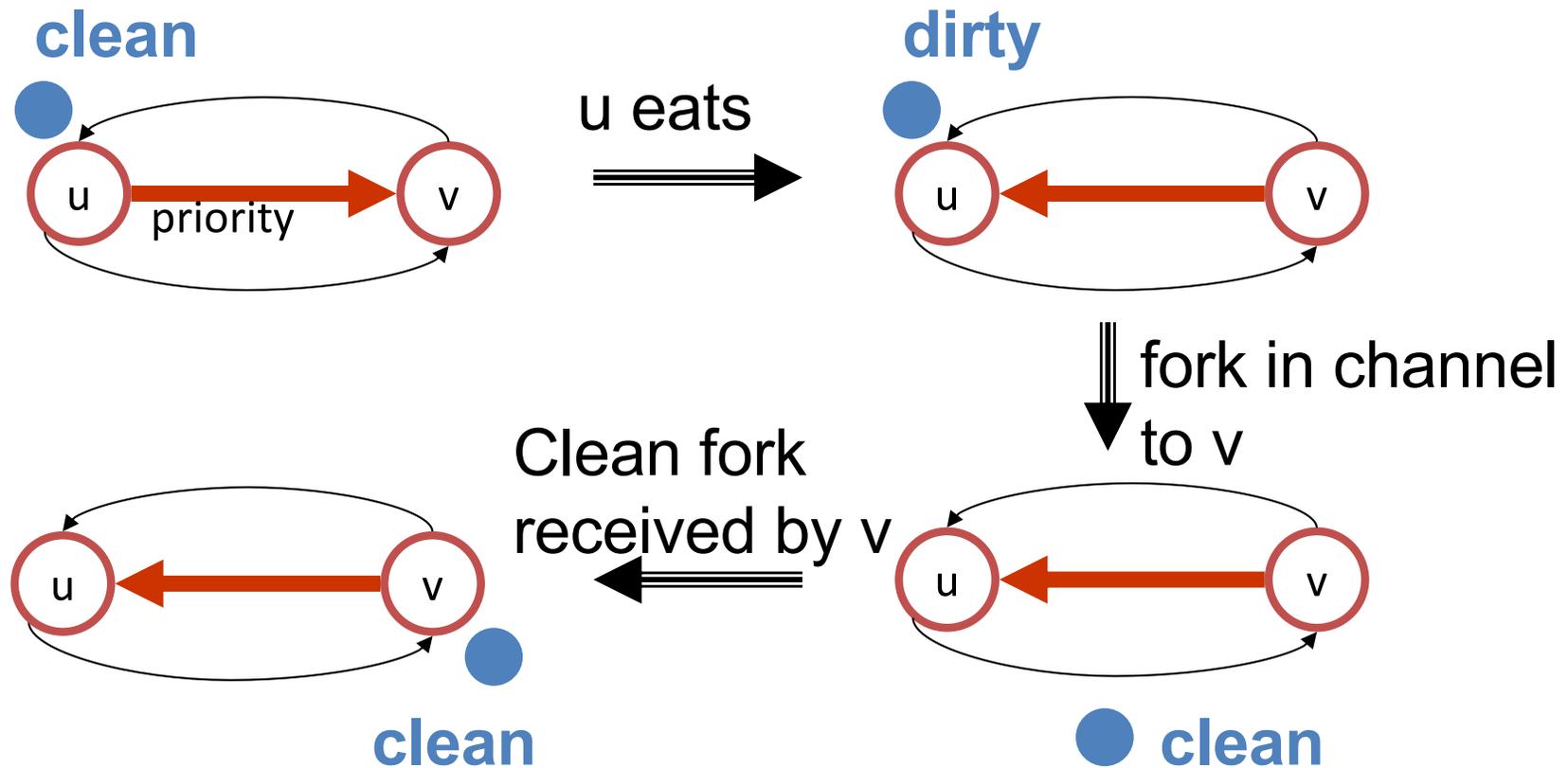
What should happen to edge directions after v eats?

- Flip edges incident on v? No. may cycle.
- Make all edges directed towards v? Yes.  
Prove that the graph remains acyclic.

**How can we represent priorities in terms of forks?**

**All forks held by an eating agent are dirty.**

**An agent holding a dirty fork has lower priority.**



**Priority changes only when a clean fork becomes dirty**

- **The key question:** What does a hungry philosopher  $u$ , who holds fork  $(u,v)$ , do when it gets a request from a neighbor  $v$ ?
- If fork  $(u,v)$  is clean then  $u$  holds the fork: it has priority; if the fork is dirty then  $u$  sends the (cleaned) fork to  $v$ .
- What does an eating philosopher  $u$  do when it gets a request for fork  $(u,v)$ ?
- Yields the fork when eating completes.

- What does a thinking philosopher  $u$ , who holds fork  $(u,v)$ , do when it gets a request from a neighbor  $v$ ?
- Thinking philosophers must yield forks because thinking philosophers may think forever, and must not hold forks forever.
- So, we must establish the following property:  
**Always: thinking philosophers do not hold clean forks. (They may hold dirty forks.)**

Next class: Write program and prove correctness

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2. **Dynamically changing graphs** to design distributed algorithms. This lecture: Priority Graphs. **Earlier lectures: Tree for Diffusing Computation. Snapshot: timeline graph.**
3. Use of **tokens** and other invariant structures. **Previous lectures also emphasized always properties.**