



Computer Lab 2 TuLiP: A Software Toolbox for Temporal Logic Planning

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Outline

- Overview of TuLiP
- Computer Lab

Problem Description

Problem: Given a plant model and an LTL specification φ , design a controller to ensure that any execution of the system satisfies φ

- The evolution of the system is described by differential/difference equations

$$s(t+1) = As(t) + Bu(t) + Ed(t))$$

$$u(t) \in U$$

$$d(t) \in D$$

where $s \in \mathbb{R}^n, U \subseteq \mathbb{R}^m, D \subseteq \mathbb{R}^p$

- φ must be satisfied regardless of the environment in which the system operates
- Assume that φ is of the form

$$\varphi = \begin{pmatrix} \psi_{init}^{e} & \wedge & \Box \psi_{s}^{e} \wedge \bigwedge_{i \in I_{f}} \Box \Diamond \psi_{f,i}^{e} \end{pmatrix} \implies \begin{pmatrix} \psi_{init}^{s} \wedge \Box \psi_{s}^{s} \wedge \bigwedge_{i \in I_{g}} \Box \Diamond \psi_{g,i}^{s} \end{pmatrix}$$
assumptions on initial condition
assumptions on environment
desired behavior

Embedded Control Software Synthesis

Key elements to specify the problem

- discrete system state
- continuous system state
- (discrete) environment state
- specification



Hierarchical Approach

- Discrete planner computes the next cell to go to in order to satisfy φ
 - The synthesis algorithm considers all the possible behaviors of the environment
 - **Issue**: state explosion
- Continuous controller simulates the plan
 - Constrained optimal control problem
 - Continuous execution preserves the correctness of the plan

Main Steps



- Generate a proposition preserving partition of the continuous state space
 - cont_partition = tlp.abstract.prop2part(cont_state_space, cont_props)
- Discretize the continuous state space based on the evolution of the continuous state
 - disc_dynamics = tlp.abstract.discretize(cont_partition, sys_dyn, N=8, ...)
- Digital design synthesis
 - specs = tlp.spec.GRSpec(env_vars, sys_vars, env_init, sys_init, env_safe, ...)
 - ctrl = tlp.synth.synthesize(specs, sys=disc_dynamics.ts, ignore_sys_init=True)
- Simulate (not yet implemented; code manually for now)
 - tlp.abstract.simulate(sys, ctrl)

Example #1: robot_simple_discrete.py

System Model: Robot can move to the cells that share a face with the current cell

Desired Properties

- Visit the blue cell infinitely often
- Eventually go to the red cell when a PARK signal is received

Assumption

- Infinitely often, PARK signal is not received

$$\varphi = \Box \diamondsuit (\neg park) \implies (\Box \diamondsuit (s \in C_5) \land \Box (park \implies \diamondsuit (s \in C_0)))$$

This spec is not a GR[1] formula

- Introduce an auxiliary variable *X0reach* that starts with True
- $\Box(\bigcirc X0reach = (s \in C_0 \lor (X0reach \land \neg park)))$
- $\Box \Diamond X0reach$



Example #2: robot_simple_continuous.py

Dynamics $\dot{x} = u_x, \dot{y} = u_y$ where $u_x, u_y \in [-1, 1]$

Desired Properties

- Visit the blue cell infinitely often
- Eventually go to the red cell when a PARK signal is received

Assumption

- Infinitely often, PARK signal is not received

$$\varphi = \Box \Diamond (\neg park) \implies (\Box \Diamond (s \in C_5) \land \\ \Box (park \implies \Diamond (s \in C_0)))$$

This spec is not a GR[1] formula

- Introduce an auxiliary variable *X0reach* that starts with True
- $\Box(\bigcirc X0reach = ((s \in C_0 \lor X0reach) \land \neg park))$
- $\Box \Diamond X0reach$

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Computer Exercise 1

Synthesize a reactive planner with the following specifications

System variables: X0,...,X8 -- Xi = 1 if robot in Ci, Xi = 0 otherwise. Environment variables: $obs \in \{1,4,7\}$, $park \in \{0,1\}$

Desired Properties

- •Visit the blue cell (C₈) infinitely often
- •Eventually go to the green cell (C₀) after a PARK signal is received
- •Avoid an obstacle (red cell) which can be one of the C₁, C₄, C₇ cells and can move arbitrarily

Assumption

- Infinitely often, PARK signal is not received
- The obstacle always moves to an adjacent cell

Constraints (or discrete dynamics)

•The robot can only move to an adjacent cell, i.e., a cell that shares an edge with the current cell

[]<>X8

```
X0reach ∧
[]<>X0reach ∧
[](next(X0reach)=((X0∨X0reach)∧ !park))
```

 $[](obs=0 \rightarrow !X1) \land [](obs=1 \rightarrow !X4) \land \\ [](obs=2 \rightarrow !X7)$

[]<>!park

```
\begin{array}{l} [](obs=0 \rightarrow next(obs)=1) \land \\ [](obs=1 \rightarrow (next(obs)=0 \lor next(obs)=2)) \land \\ [](obs=2 \rightarrow next(obs)=1) \end{array}
```



Computer Exercise 2

Synthesize intersection logic for the car with the following specification:

Desired Properties

- Vehicle *a* should eventually go to C9
- Vehicle a does not collide with vehicle h
- Vehicle *h* is not in the intersection when the light is red

Assumptions

- find a set of "non-trivial" assumptions that render the problem realizable
- allow human vehicle to start in any location

Constraints

 Vehicles can only move to cells representing their possible travel lanes



Validation Possibilities

Add continuous-time dynamics to intersection problem Synthesize decision-making logic for road network Automated valet parking



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 c_2