

# Specification, Design & Verification of Networked Control Systems



Richard M. Murray Ufuk Topcu
California Institute of Technology
Caltech/AFRL Short Course
24-26 April 2012

#### Goals for the course:

- Review recent applications in "protocol-based" control systems
- Provide an overview of basic tools from computer science and control theory that can be used as a basis for further studies
- Review recent results in formal methods, logic synthesis, hybrid systems and receding horizon, temporal logic planning (RHTLP)
- Discuss open research problems and emerging control applications

## Course Instructors



Richard M. Murray

Caltech

#### **Education**

- BS, Caltech, EE
- PhD UC Berkeley, EECS
- Professor, Caltech

#### **Research interests**

- Networked control
- Verification of distributed control systems
- Biological circuit design



Ufuk Topcu Caltech

#### **Education**

- MS, UC Irvine, MAE
- PhD UC Berkeley, ME
- Postdoc, Caltech

#### **Research interests**

- Distributed embedded systems
- Uncertainty quantification and management
- Optimization/control of multiscale networked systems



Tichakorn (Nok) Wongpiromsarn

MIT/Singapore

#### Education

- BS, Cornell, ME
- PhD, Caltech, ME
- Postdoc, MIT/Singapore

#### **Research interests**

 Verification and synthesis of hybrid control systems

# Comments on Style and Approach

# Protocol-based control is an emerging research area

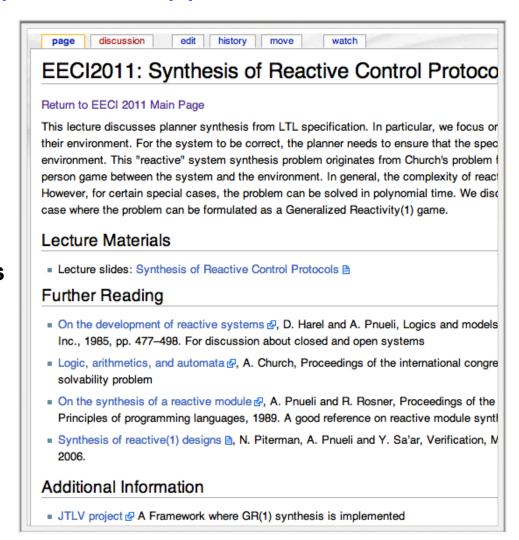
- Many results are new (in the last 5 years) and haven't yet been standardized
- Integration between different aspects of the research are a work in progress

## Course uses new language and concepts

- Basic ideas will be familiar to control researchers: stability, reachability, simulations vs proofs, etc
- Much of the terminology will be strange ("TS ⊨ □(¬b → □(a ∧ ¬b)") => ask questions if you get lost

#### Lots of additional material online

- Additional references, web pages, etc are posted on the wiki pages
- Copies of slides/lecture notes available



## Lecture Schedule

	Tue	Wed	Thu
8:30	L1: Intro to Protocol- Based Control Systems	Computer Lab 1 Spin	L8: Receding Horizon Temporal Logic Planning
10:30	L2: Automata Theory	L5: Verification of Control Protocols	Computer Lab 2 TuLiP
12:00	Lunch	Lunch	Lunch
13:30	L3: Linear Temporal Logic	L6: Hybrid Systems Verification	L9: Extensions, Applications and Open Problems
15:30	L4: Model Checking and Logic Synthesis	L7: Synthesis of Reactive Control Protocols	





# Lecture 1: Introduction to Protocol-Based Control Systems

# Richard M. Murray Caltech Control and Dynamical Systems 24 April 2012

#### Goals:

- Describe current and emerging applications of networked control systems
- Discuss the role that control "protocols" play in NCS
- Provide an overview into what we will learn in the course

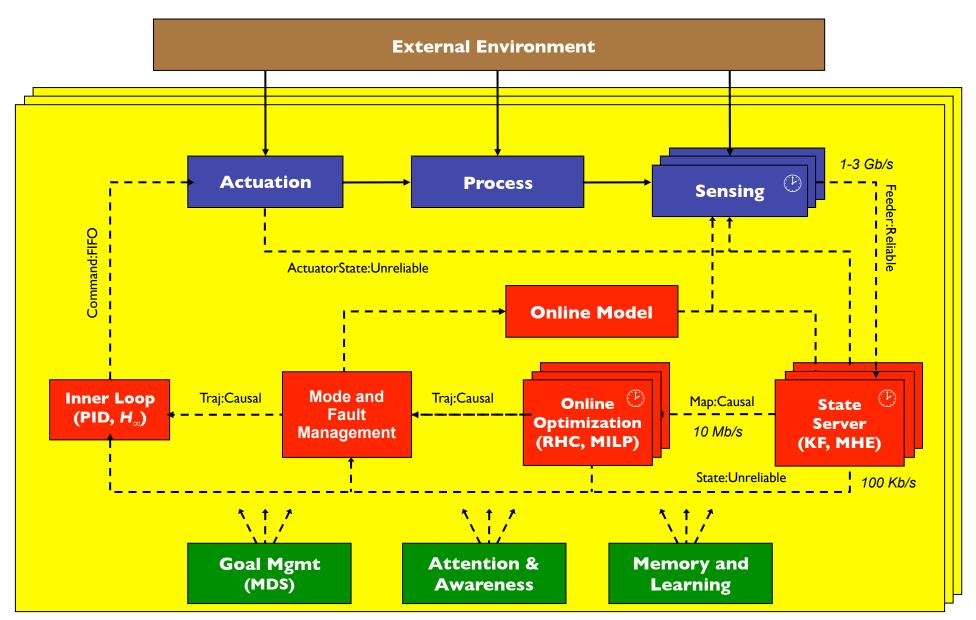
## Reading:

- Control in an Information Rich World, Sections 1, 3.2 and 3.3
- Sensing, Navigation and Reasoning Technologies for the DARPA Urban Challenge, 2007

Available on course wiki page

# Networked Control Systems

(following P. R. Kumar)



# Some Important Trends in Control in the Last Decade

## (Online) Optimization-based control

- Increased use of online optimization (MPC/RHC)
- Use knowledge of (current) constraints & environment to allow performance and adaptability

## Layering and architectures

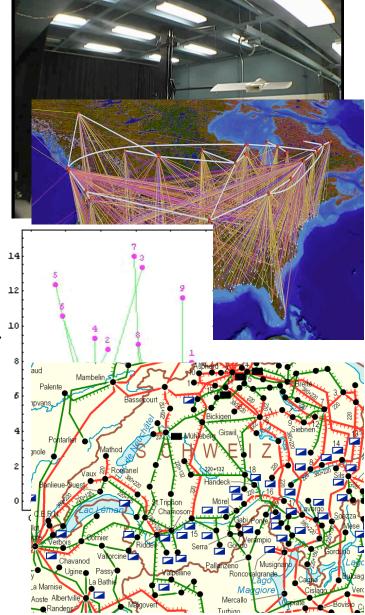
- Command & control at multiple levels of abstraction
- Modularity in product families via layers

## Formal methods for analysis, design and synthesis

- Combinations of continuous and discrete systems
- Formal methods from computer science, adapted for hybrid systems (mixed continuous & discrete states)

## Components $\rightarrow$ Systems $\rightarrow$ Enterprise

- Movement of control techniques from "inner loop" to "outer loop" to entire enterprise (eg, supply chains)
- Use of systematic modeling, analysis and synthesis techniques at all levels
- Integration of "software" with "controls" (Internet of things, cyber-physical systems, etc)





# Motivating Example: Alice (DGC07)

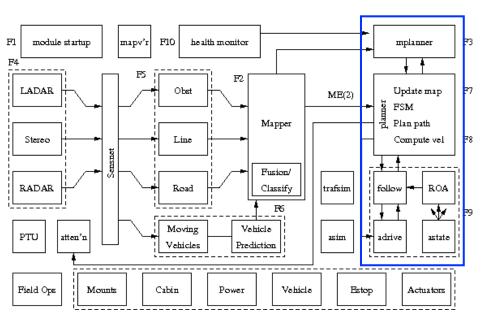


#### **Alice**

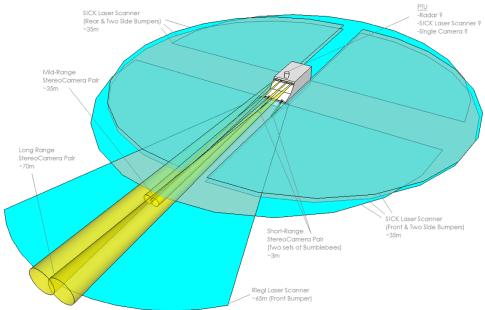
- 300+ miles of fully autonomous driving
- 8 cameras, 8 LADAR, 2 RADAR
- 12 Core 2 Duo CPUs + Quad Core
- ~75 person team over 18 months

#### **Software**

- 25 programs with ~200 exec threads
- 237,467 lines of executable code









## Planner Stack



## Mission Planner performs high level decision-making

Burdick et al, 2007

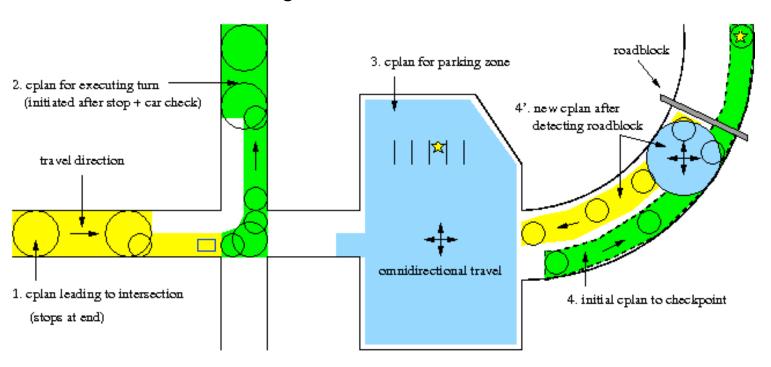
Graph search for best routes; replan if routes are blocked

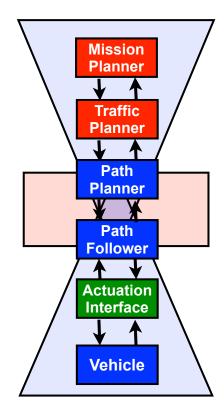
#### Traffic Planner handles rules of the road

- Control execution of path following & planning (multi-point turns)
- Encode traffic rules when can we change lanes, proceed thru intersection, etc

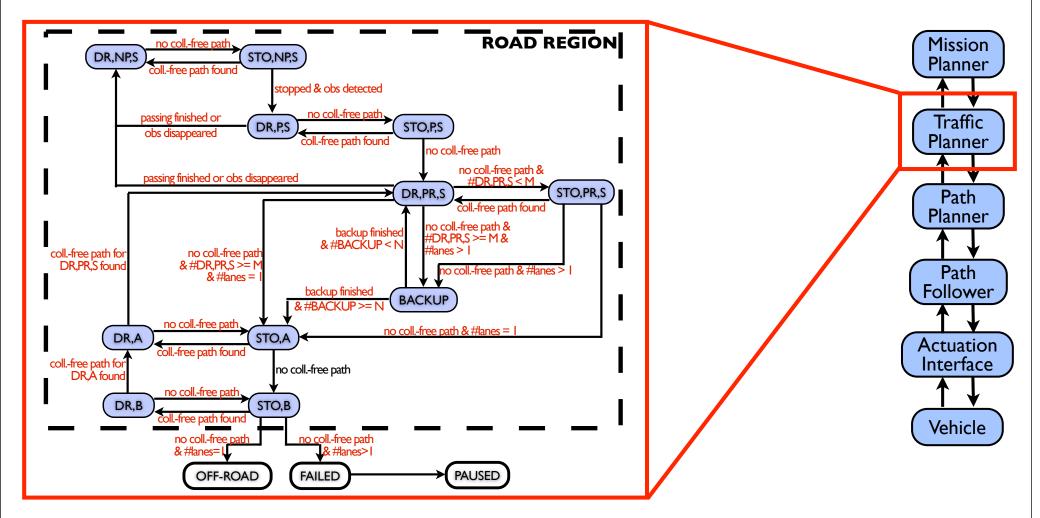
## Path Planner/Path Follower generate trajectories and track them

- Optimized trajectory generation + PID control (w/ anti-windup)
- Substantial control logic to handle failures, command interface, etc.





# Traffic Planner Logic



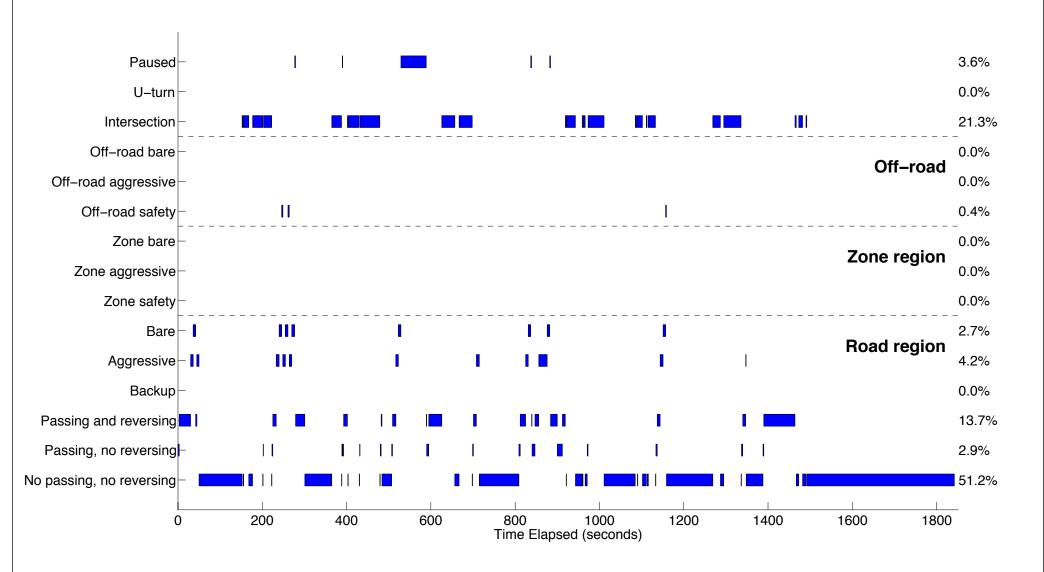
## Goal: move from verification of human-designed FSA (hard!) to synthesis

- Given specification + model of the environment, can we produce the FSA?
- Key enabler: new tools in logic synthesis (eg, Kress-Gazit & Pappas, Sa'ar)



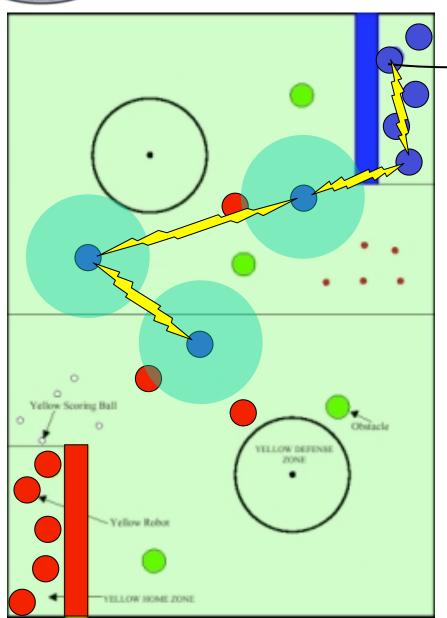
## Mode Transitions

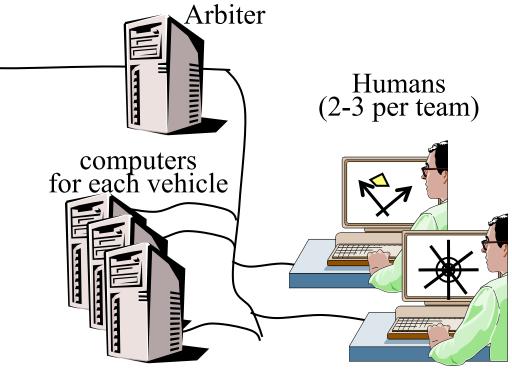






# Example: RoboFlag (D'Andrea, Cornell)





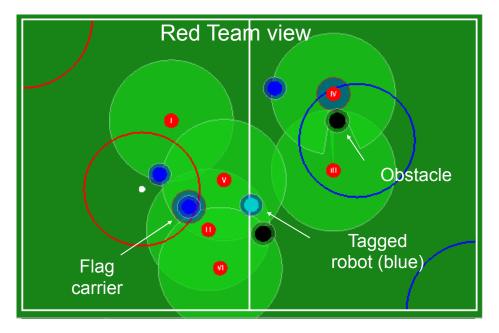
## Robot version of "Capture the Flag"

- Teams try to capture flag of opposing team without getting tagged
- Mixed initiative system: two humans controlling up to 6-10 robots
- Limited BW comms + limited sensing



# RoboFlag Demonstration





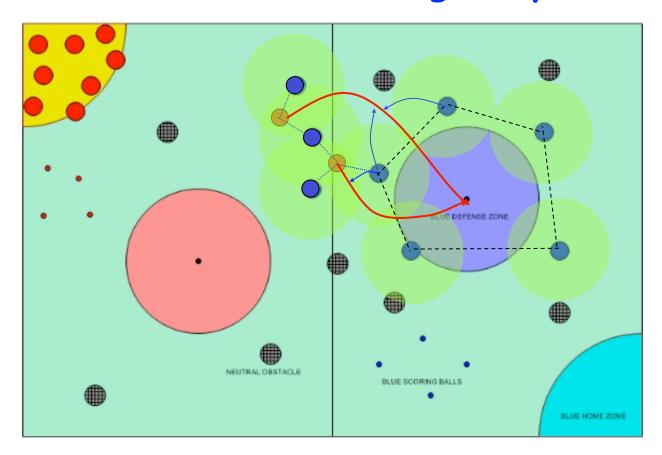
## Integration of computer science, communications, and control

- Time scales don't allow standard abstractions to isolate disciplines
- Example: how do we maintain a consistent, shared view of the field?

## Higher levels of decision making and mixed initiative systems

- Where do we put the humans in the loop? what do we present to them?
- Example: predict "plays" by the other team, predict next step, and react

# RoboFlag Subproblems



#### 1. Formation control

Maintain positions to guard defense zone

#### 2.Distributed estimation

 Fuse sensor data to determine opponent location

#### 3. Distributed consensus

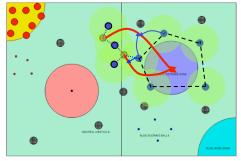
Assign individuals to tag incoming vehicles

## Goal: develop systematic techniques for solving subproblems

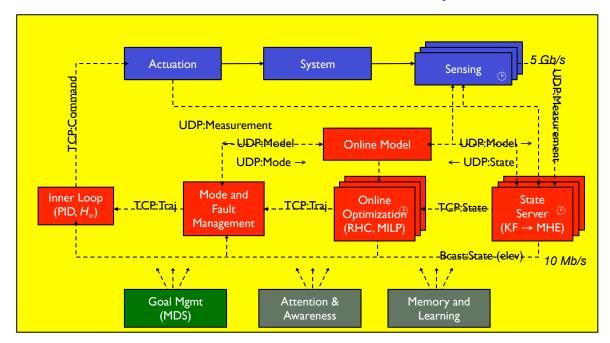
- Cooperative control and graph Laplacians
- Distributed estimation and sensor fusion
- Distributed receding horizon control
- Packet-based estimation and control
- Verifiable protocols for consensus and control

Implement and test as part of annual RoboFlag competition

# Summary: Protocol-Based Control Systems







## **Control Challenges**

- How should we distribute computing load burden between computers?
- How should we handle communication limits and dropped packets?
- How do multiple computers cooperate in a shared task (with common view)?
- What types of protocols should we use for making correct (safe) decisions?

## **Specification**

How do we describe correct behavior?

## Design

 What tools can we use to design protocols to implement that behavior?

#### Verification

How do we know if it is actually correct?

## **Synthesis**

Can we generate protocols from specs?

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