

$$S_{r_0} = \left\{ r \in M \mid \langle \langle r - r_0, \xi_M(r_0) \rangle \rangle = 0, \text{ for all } \xi \in \mathfrak{g} \right\}$$