

$$S = g^{-1} \dot{g} \in \mathfrak{g}$$