

$$P_n u(x, t) = \sum_{j=1}^n a_j(t) \varphi_j(c(t)x)$$