

$$\tilde{\mathbf{q}}(x,y,t) = \mathbf{u}_0(y) + \sum_{j=1}^n a_j(t)\varphi_j(x,y)$$