

$$\frac{\dot{g}}{g} = \frac{\langle f_g^1(\tilde{u}), y \partial_y u_0 \rangle}{\langle y \partial_y \tilde{u}, y \partial_y u_0 \rangle}$$