Errata: Nonholonomic Mechanics and Control

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This file contains the errata known to us as of the above date for the *first printing* of the 1st edition (2003). These errata will be corrected in the *second printing*.

Introduction

Page 1, Line 11 : Insert a closing parenthesis after "whole" and a comma after "law".

- **Pages 6,7 Section 1.2** : Interchange a and b in the endpoints of the integrals for consistency.
- Page 9, first line of paragraph "Energy and Hamilton's Equations" : There is a missing partial before \dot{q}_i .
- **Page 10, 3rd last line, last displayed equation** : Replace Γ_r^{lm} with Γ_{rlm} .
- **Page 11, 5 lines from bottom** : F^i should be F_i .
- Page 18, displayed equation lines before displayed equation (1.4.4): Second equation should have an m before the R^2 .
- Page 20, equation (1.4.9) : This equation should read

 $J\ddot{\varphi} - R\mu_1 \dot{\theta}\sin\varphi + R\mu_2 \dot{\theta}\cos\varphi = u_{\varphi}$

- **Page 23, Figure 1.6.1** : Interchange x and y on the axes.
- Page 26, Line 8 : J should be I.
- **Page 27, 8 lines after (1.7.4)** : Replace "and one negative eigenvalue" with "together with a negative eigenvalue if v > 0 and a positive eigenvalue if v < 0."
- **Page 27, Figure 1.7.2**: Labeling of axes should be interchanged i.e. v and ω should be swapped.
- **Page 30, Equation (1.8.8)** : $xu_2 yu_1$ should read $yu_1 xu_2$.
- **Page 32, First line after second display** : Replace x by q, three times.
- **Page 33, Three lines below equation (1.8.16)** : $\dot{z} = x\dot{y} y\dot{x}$ should be $\dot{z} = y\dot{x} x\dot{y}$.
- Page 34, Lines 4 and 5 : Remove the minus signs in both places.
- **Page 34, Two lines below (1.8.17)** : In the display, ta^2 should be $a/2\pi$.
- Page 36, 37 First equation of (1.9.8) and of (1.9.9) : Multiply λ_1 and λ_2 by *a*. Also, on the first and last line of (1.9.9), $\hat{\omega}$ should be boldface: $\hat{\omega}$.

Page 39, Equation (1.9.21) : Eliminate the extra parenthesis right after K.

- **Page 45, Displayed equation for** *H* **above (1.12.1)** : The parenthesis at the end of this line should not be a subscript; i.e. x_{k+1} should be x_{k+1}).
- **Page 46, Displayed equation for** *B* **below (1.12.6)** : In the last row of the matrix *B*, a_{n-1} should be $-a_{n-1}$

Chapter 2

Page 59, first line of Proposition 2.1.9 : (M) should be (U).

- **Page 60, fifth line from the bottom** : "level set of X" should be " level set of f"
- **Pages 63, 64** : various occurrences of " ϕ " should be " φ " to be consistent with the figure.
- **Page 64, Paragaph in middle** : The title of the paragraph should be "Level Sets as Differentiable Manifolds in \mathbb{R}^n .
- **Page 68, equation (2.2.1)** : After Df(u) there should be a \cdot not a comma.
- Page 74, title of section 2.4 : Title should be "Center Manfolds" and the words "Theory and the Lyapunov-Malkin Theorem" should be removed from the first line of the section.
- **Page 75, Theorem 2.4.3 should read** : Suppose that the zero solution of (2.4.3) is stable (resp. asymptotically stable) and that the eigenvalues of A are in the left half-plane. Then the zero solution of (2.4.1, 2.4.2) is stable (resp. asymptotically stable). If either the zero solution of (2.4.3) is unstable, or if any eigenvalues of A are in the right half plane, then the zero solution of (2.4.1, 2.4.2) is also unstable.
- **Page 78: Exercise 2.4.1** In the first line of displayed equation, y^2 should be xy. There is a similar correction in the caption of the accompanying figure 2.4.2.
- **Page 85, 4th line of exercise 2.5-2** : x, y, z should all in the denominator with with ∂ .
- Page 87, 2nd last line : "Jacobi Lie bracket" repeated (index problem).
- **Page 91, item number 14** : x, x_1, \ldots, x_k should be X, X_1, \ldots, X_k . Also, the summation on the index *i* should start at 1, not zero.
- **Page 92: Exercise 2.6-1** : There is a lettering problem: remove the (a) (this is not an exercise). Then (b) should be (a) as so on. Also the β is the current part (e) should α .
- Page 98: Two lines above Definition 2.8.5 : "The by lemma..." should read "Thus, by the preceding lemma,..."
- Page 99, two lines after (2.8.1) : "if and if only if" should be "if and only if"

Page 100, End of first paragraph : SO(n) should be $\mathfrak{so}(n)$.

Page 103, Definition 2.8.13 : Rewrite the definition as follows: Suppose $\Phi : G \times M \to M$ is an action. For $\xi \in \mathfrak{g}$, the map $\Phi^{\xi} : \mathbb{R} \times M \to M$ defined by $\Phi^{\xi}(t, x) = \Phi(\exp(t\xi), x)$ is an \mathbb{R} -action—that is, a flow—on M. The vector field on M that generates this flow, namely

$$\xi_M(x) = \left. \frac{d}{dt} \right|_{t=0} \Phi^{\xi}(t,x) \,. \tag{2.8.3}$$

is called the *infinitesimal generator* of the action corresponding to ξ .

Page 105, Defn 2.9.1 (ii) second line : insert a comma after U_k .

Page 112, 12th line : Middle term in curly parentheses should have g_{lk} not g_{ik} .

Chapter 3

Page 122: Last displayed formula : P_i should be p_i .

- **Page 137: Line after (3.7.5)** : $\xi_Q(q^i)$... should be $\xi_Q(q)$
- Page 143: 4 lines after displayed equation (3.9.5) : Delete the minus sign in front of $\nabla \times \mathbf{A}$.
- Page 146: equation (3.10.18) should read as follows (swap the arguments on the right hand side):

$$\operatorname{ver}_{q} v = [\mathcal{A}(q, v)]_{Q}(q) = \left(\dot{s} - \frac{\beta}{\gamma}\cos\theta\dot{\theta}, 0\right),$$
$$\operatorname{hor}_{q} v = v - \operatorname{ver}_{q} v = \left(\frac{\beta}{\gamma}\cos\theta\dot{\theta}, \dot{\theta}\right)$$

and the A at the end of the example should be \mathcal{A} .

Page 162, equation (3.13.11) : Last term in square brackets should be squared; i.e. $||\dot{\mathbf{r}}_1||^2$.

Chapter 4

Page 180, Line below (4.2.7) : Delete the duplicate appearance of $[g_2, [g_1, f]](\Omega)$.

Page 205, equation (4.6.18) : Delete the last parenthesis.

Chapter 5

Page 217, two lines before(5.2.3) : Instead of "choose, in a neigborhood of each point, a local coordinate chart..." put rather "choose local coordinates"

Chapter 7

Page 331, line after (7.1.4) : One "of" should be deleted.

Page 343, Assumption (ii) : Replace "The dimension of D_F is" by "The dimension of the distribution D_F defined by the span of X_1, \ldots, X_k is"

Chapter 8

Page 392, Line following equation (8.6.1) : $p = I_{ab}\omega^b$ should be $p_a = I_{ab}\omega^b$.

Chapter 9

Page 403, equation (9.2.2) and the following displayed equation : λ^2 should be λ_2 and $\frac{1}{2}l_3^2$ should be $\frac{l_3^2}{2J_3}$.

Page 403, fourth line from the bottom : Π_2 should be Π_3 .

Page 405, tenth line : Close parentheses after "below".

Bibliography

Page 440, Appell 1911 reference : "lews" should be "les",

Page 444 : Add [1985] to the Burke reference.

- Page 452, Helmke reference : Authors in the reference should be Hemlke, U. and J. Moore.
- Page 463, Rumiantsev 1966 reference : Valentin should be V. for consistency.
- More References : See the book's website http://www.cds.caltech.edu/mechanics_ and_control/ for additional bibliography