# Errata: Mechanics and Symmetry 

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December 11, 1996

We appreciate being informed about additional corrections. We do not include all stylistic or spelling corrections in this list. Additional corrections can be sent to marsden@cds.caltech.edu. We are especially grateful to Anthony Bloch, Hermann Flaschka, Meinhard Mayer, Peter Mucha, Juan-Pablo Ortega, and other readers for notifying us of corrections.

## Errata

## Chapter 1-Introduction and Overview

- Page 2, 4 lines before equation (1.1.1): the second $L$ should have a dependence on $t$ included.
- Page 4, In equation (1.1.14): the $\partial$ in the denominators of the right hand sides of equations should be $\delta$.
- Page 9, the equation displayed after equation (1.3.2): the $c$ should be $C$.
- Page 13, In the third paragraph: delete the reference to Chapter 13 (this chapter will appear in a future volume).
- Page 14, line 1: add a question mark at the end of the line.
- Page 20 , the line after (1.6.6) should read: "where $\delta F / \delta \mathbf{E}$ and $\delta F / \delta \mathbf{B}$ are vector fields with $\delta F / \delta \mathbf{B}$ divergence free defined in the" and two lines after (1.6.7), delete the "div".
- Page 34 , on the bottom line: $\mathbf{1 . 1 0 - 3}$ should be $\mathbf{1 . 1 0 - 4}$.
- Page 36 , line $4 \uparrow: \varphi$ should be $\theta$.


## Chapter 2-Hamiltonian Systems on Linear Symplectic Spaces

- Page 52, line 7: Crough should be Crouch.
- Page 61: (2.4.10) should be to the preceding display.
- Page 62 , in the line right after the box: the first $\Omega$ should be $\Omega_{z}$.
- Page 67, in 2.6-1(b): omit the part of the first sentence preceding "show that".
- Page 68, line following equation (2.7.7): the reference to 3.1 should be to 3.2 .
- Page 69, line $7 \uparrow$ : omit the first (.
- Page 70, in Exercise 2.7-3: $\phi$ should be assumed to be a linear symplectic map.
- Page 74, on line $6 \uparrow$ : insert a minus sign after the last equals sign.
- Page 78, line $8:$ insert ] before the $\}$.
- Page 81, in the lower part of Figure 2.10.4: the arrows on the right hand side are going in the wrong direction.
- Page 83, the line after (2.11.4) should read: "From this point of view, $\theta$ gets identified with time and the curve", two lines below this, (2.11.2) should be (2.11.4) and on line $5 \uparrow, \bar{x}_{0}(0)$ should be $\bar{x}(0)$.
- Page 83 The proof of Theorem 2.11.1 requires corrections: please request the corrected file if needed.
- Page 86, Example C(iii): add a (before "transversal".


## Chapter 3-An Introduction to Infinite-Dimensional Systems

- Page 99, in line 5: the $H$ should be $H_{1}$ and in line $4 \uparrow, H$ should be $h$.
- Page 100 , in line $2 \uparrow: u_{t} d^{3} x$ should be $u_{t} d x$.
- Page 104, in (3.3.6): $P_{x}(\varphi)$ should be $P_{x}(\varphi, \pi)$.
- Page 105, on line 3: $\S 3.3$ should be $\S 3.2$. In (3.3.11) delete the period.
- Page 107 , in $F_{1}$ : the $u^{3}$ should be $u^{2}$ and in $F_{3}$ the first plus should be a minus, and there should be a factor of $\frac{1}{2}$ in front of the $\left(u_{x x}\right)^{2}$ term.


## Chapter 4-Interlude: Manifolds, Vector Fields, Differential Forms

- Page 117, line 7: 4.2.4ii should be 4.2.4iv.
- Page 119, last line of $1(\mathrm{a})$ in the box: $\mathbf{e}^{3}$ should be $\mathbf{e}_{3}$.
- Page 121, in (4.3.5) : add $(x)$ at the end of the equation.
- Page 122 , in line $7 \uparrow: \mu$ should be $\mu_{2}$ and in the next line, $Q$ should be a zero.


## Chapter 5-Hamiltonian Systems on Symplectic Manifolds

- Page 133, in line $2 \uparrow$ and in (5.1.3): replace $[n / 2]$ by $n(n-1) / 2$.
- Page 134, In the line following (5.2.1): $P$ should be $P_{1}$.
- Page 143, Just below the middle of the page, in the last line of the display: $\Omega_{z}^{*}$ should be $\Omega_{z}^{b}$.
- Page 146, At the end: 5.4-2 should be 5.4-3.


## Chapter 6-Cotangent Bundles

- Page 149, In line $8 \uparrow$ : 6.1 .6 should be $\mathbf{6 . 1 . 1}$.
- Page 151, In line 12: $\alpha_{i}$ should be $\alpha_{j}$ and three lines below that, $B^{i}$ should be $B^{j}$ (twice) and $=p_{i}^{0}$ should be $p_{j}^{0}$.
- Page 152, Exercise 6.6.2: add " $0 \mathbf{d} f$ " to the end of the line.
- Page 154, In line 3: Delete the extra)
- Page 162: Replace the sentence after (6.8.1) "However, one really,..." by "However, at a fixed point, one really wants to use the given symplectic form evaluated at the fixed point, which has the expression $d\left(\delta q^{i}\right) \wedge$ $d\left(\delta p_{i}\right),(6.8 .2)$ while (6.8.1) restricts to zero."
- Page 164: Delete the text from line $9 \uparrow$ to the third line after (6.8.11) on page 165. Also delete the last sentence of the paragraph including formula (6.8.12).


## Chapter 7-Lagrangian Mechanics

- Page 166: the $\partial$ in the first line of (6.8.16) for $d p_{i} / d t$ should be a $d$ and in the third line, $w^{i}$ should be $w_{i}$.
- Page 182 , line $2 \uparrow$ : add a ) before the right hand angle bracket.
- Page 191, Section 7.9 has been rewritten: if you are reading this section, please request a revised copy from the authors.
- Page 198, line 1: 7.8-2 should be 7.9-2


## Chapter 8-Variational Principles, Constraints, Rotating Systems

- Page 219, In problem 8.1-2: insert a minus sign in front of the right hand side.


## Chapter 9-An Introduction to Lie Groups

- Page 244, on the last line: $\phi_{2}$ should be $\phi_{g_{2}}$ and $\phi_{1}$ should be $\phi_{g_{1}}$.
- Page 245: the two $g$ 's in the left hand side of the figure should be $h$ 's.
- Page 251 , in the first line of Example (b): it should be $\mathfrak{g}=L\left(\mathbb{R}^{n}, \mathbb{R}^{n}\right)$.
- Page 255, in line $3 \uparrow: \phi(x)$ should be $\phi^{-1}(x)$ and in the second line of the remark, banach should have a capital B.
- Page 258 , in line $3 \uparrow: a_{4}^{2}$ should be $a_{3}^{2}$.
- Page 259 , in line $3: \mathbb{R}$ should be $\mathbb{R}^{3}$ and in the 4 th line of the proof of $9.2 .5,|\lambda|$ should be $|\lambda|^{2}$.
- Page 261, in the line above (9.2.7): the superscript $2 n-1$, should be $n-1$.
- Page 262, in the first line of Proposition 9.2.8: "nonconnected" should read "connected".
- Page 263, line 5 at the end of the line: in the expression for $A^{T}$, swap $w$ and $z$.
- Page 265: the last $x$ in the first display should be $z$.
- Page 270, in line 2 of (b): delete the redundant "for $\mathbf{x} \in \mathbb{R}^{3}$ and $A \in S O(3)$ ".
- Page 274, in line 4: $\Phi_{g}\left(\exp t \xi, \Phi_{g^{-1}}(x)\right)$ should be $\left(\Phi_{g} \circ \Phi_{\exp t \xi^{\circ}} \circ \Phi_{g^{-1}}\right)(x)$.
- Page 276, in line 5 of Remark 3: the second Ad should be ad.
- Page 277, three lines above part (c): $\mathfrak{l}=\{B \in$ should be $\mathfrak{l}=\{A \in$.
- Page 279, line $3 \uparrow: \eta(0)=\eta$ should be $\eta(0)=0$.


## Chapter 10-Poisson Manifolds

- Page 289, In (10.2.13): the last a should be b.
- Page 290, In the first line of Exercise 10.2-4: change $G$ to $H$.
- Page 297, line 4 of Proposition 10.5.2: the last $=$ should be $\in$.
- Page 299-300, 307-308, 313: the symbols $\mathcal{L}$ should be $£ \quad$ (the Lie derivative).
- Page 307, in Exercise 10.6-2: delete the reference to the nonexistent exercise 5.5-4.
- Page 308, line 2: multiply the second term on the right hand side by $F$ and the third by $G$.
- Page 309 , line $8 \uparrow$ : the sub $\pi$ should be on line.
- Page 315, in line 9: $z$ should be $Z$.
- Page 317, at the end of line 4: $T_{x} M$ should be $T_{x}^{*} M$.
- Page 320, in (10.9.13): the second two $\mu$ 's should be $\nu$ 's.
- Page 321 , in line $3 \uparrow: B(\mu)$ should be $\langle\cdot, \mu\rangle$.
- Page 321 , on lines 4 and $8 \uparrow: V$ should be $V^{*}$.


## Chapter 11-Momentum Maps

- Page 328: $J$ should be J.
- Page 330, in Exercise 11.4-1: the reference should be to equation (10.7.3).
- Page 331: insert a minus after the last $=$ in (11.5.6) and in line $5 \uparrow$, ( $\mathbf{p}$ ) should be ( $\mathbf{q}, \mathbf{p}$ ).
- Page 333, second line after (11.5.16): $\mathfrak{g}^{*}$ should be $\mathfrak{g}$.


## Chapter 12-Computation and Properties of Momentum Maps

- Page 340 , line $8 \uparrow$ : add (at the beginning of the line.
- Page 342, line $2 \uparrow$ : the last $g \cdot \alpha_{q}$ should be $g \cdot q$.
- Page 344, line 12: $\xi_{P}(p)=d /\left.d t\right|_{t=0} T_{p} \varphi_{t}$ should be $\xi_{P}\left(v_{q}\right)=d /\left.d t\right|_{t=0} T_{q} \varphi_{t}\left(v_{q}\right)$.
- Page 345 , in (12.3.1): $N$ should be $3 N$.
- Page 351, in Exercise 12.3-4: in the integral, the $J$ should be bold.
- Page 352, line 7: the (after the second $=$ should be $\langle$.
- Page 356 , on the line after (12.4.26): the $\mathfrak{g}$ should have a prime on it.
- Page 360, in Exercise 12.5-3: $F_{F \circ J}$ should be $X_{F \circ J}$ and the last $J$ on the line should be bold.


## Chapter 13-Euler-Poincaré and Lie-Poisson Reduction

- Page 371 , line $10 \uparrow: \xi_{Q}$ should be $\xi_{G}$.
- Page 379, line 8 : $T_{g(t)}^{*} L$ should be $T_{e}^{*} L_{g(t)}$.
- Page 380, the proof of 13.6 .2 is incomplete: please ask the authors for the complete proof if needed.
- Page 392, line $6 \uparrow: \partial x^{b}$ should be $\partial \xi^{b}$.
- Page 395, three lines after (13.8.22): delete the minus $\operatorname{sign}$ in $u_{t}=$ -....


## Chapter 14-Coadjoint Orbits

- Page 400 , in the first line of (14.1.1): $\mathbf{A}^{-1} \hat{\mathbf{v}}$ should be $\left(\mathbf{A}^{-1} \mathbf{v}\right)$.
- Page 401, in the line above Example (c): $\beta$-axis should be $\alpha$-axis.
- Page 413 , at the end of Example (b): the expression for the orbit symplectic structure should be $\omega^{-}=(1 / \beta) d \alpha \wedge d \beta$ and on the preceding line, "in coordinates $(q, p)$ " should be "in coordinates $(\alpha, \beta)$."
- Page 421, in line 8: "ab" should be "ad".
- Page 423 , in (14.8.12): the matrix associated with $\mathbf{X}_{2}$ should be $\left[\begin{array}{ll}0 & 1 \\ 1 & 0\end{array}\right]$ and in the right hand part of figure 14.8.1, the axes should be relabeled: $a$ should be $c, c$ should be $a-b$ and $b$ should be $a+b$. In the caption, $\mathfrak{s e}(3)^{*}$ should be $\mathfrak{s e}(2)^{*}$.
- Page 430, in Exercise 14.9-3: on the last row of the matrix $g$, interchange $a$ and $b$ and add the condition $|a|^{2}-|b|^{2}=1$.


## Chapter 15-The Free Rigid Body

- Page 437: Figure 15.3.1 (and on the cover) shows the case $I_{1}<I_{2}<I_{3}$. Add this to the figure caption.
- Page 438 , in equation (15.4.6): delete the stray apostrophe.
- Page 450: The sum preceding (15.9.4) should start at $i=1$.
- Page 451, on line 9: longest should be shortest.
- Page 451 , on line 16 : short should be long.
- Page 455, in the expression for $a_{66}$ on the line following (15.10.7): there should be a factor of 2 in front of the last term, $\Pi_{3}^{0} d$.
- Page 456, in the second displayed equation: the second factor (multiplying the big squared term) should be

$$
\left[a_{66}\left(\frac{1}{I_{3}}+a+c\right)-a_{36}^{2}\right]
$$

- Page 456: equation (15.10.10) should read

$$
a_{66}\left(\frac{1}{I_{3}}+a+c\right)-\left(\dot{\Phi}\left(\Pi_{3}^{0}, 1\right)+\Pi_{3}^{0} c+d\right)^{2}>0
$$

- Add the following to the references: Bloch, A.M., H. Flaschka, and T.S. Ratiu [1993] A Schur-Horn-Kostant convexity theorem for the diffeomorphism group of the annulus. Inv. Math. 113, 511-529.

